

1 **A window into the complexity of the dynamic rupture of the 2011 Mw 9**

2 **Tohoku-Oki earthquake**

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21 **Abstract:**

22 The 2011 Mw 9 Tohoku-Oki earthquake, the best recorded earthquake in the history
23 of seismology, provides unique opportunities to address fundamental issues in
24 earthquake source dynamics. Here we conduct a high resolution array analysis based
25 on recordings from the USarray and the European network. The mutually consistent
26 results from both arrays reveal unprecedentedly observed rupture complexity,
27 involving phases of diverse rupture speed and intermittent high frequency bursts
28 within slow speed phases, which suggests spatially heterogeneous material properties.
29 The earthquake initially propagates down-dip, with a slow initiation phase followed
30 by sustained propagation at speeds of 3 km/s. The rupture then slows down to 1.5
31 km/s for 60 seconds. A rich sequence of bursts is generated along the rim of this slow
32 and roughly circular rupture front. Before the end of the slow phase an extremely fast
33 rupture front detaches at about 5 km/s towards the North. Finally a fast rupture front
34 propagates towards the south running at about 2.5 km/s for over 100 km. Key features
35 of the rupture process are confirmed by the strong motion data recorded by K-net and
36 KIK-net. The energetic high frequency radiation episodes within a slow rupture phase
37 suggests a patchy image of the brittle-ductile transition zone, composed of discrete
38 brittle asperities within a ductile matrix. The high frequency is generated mainly at the
39 down-dip edge of the principal slip regions constrained by geodesy, suggesting a
40 variation along dip of the mechanical properties of the mega thrust fault or their
41 spatial heterogeneity that affects rise time.

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1. Introduction

The Mw 9 earthquake that occurred off-shore Tohoku, Japan, on March 11 2011 is by far the best recorded earthquake in the history of seismology and will undoubtedly spawn a broad range of studies that will deeply transform earthquake science. In particular, this event provides a unique opportunity to address, through high resolution and robust observations, fundamental questions about the physics of dynamic earthquake rupture, including the initiation of rupture, the complexity of its propagation and its arrest. Here we focus on key direct observations of the spatio-temporal evolution of the rupture process of the Tohoku earthquake. We analyze seismic data available soon after the event using source imaging methods that are weakly dependent on model assumptions. We back-projected teleseismic waveforms applying high-resolution array processing techniques to obtain a high-frequency image of the rupture process of this mega-earthquake. We then identified prominent features of the local strong-motion recordings that we associate to the main phases of the rupture process. Our results reveal, with unprecedented detail, rich patterns of high frequency radiation from the deep portions of the seismogenic zone. Our observations open a direct window into the complexity of dynamic rupture, including phases of slow and extremely fast rupture, and its relation to the heterogeneous nature of the subduction interface.

Back-projection of high-frequency (HF) seismic waves recorded by dense arrays [Fletcher *et al.*, 2006; Ishii *et al.*, 2005] deliver unique insights on earthquake rupture

65 processes that are complementary to traditional finite source inversions. Array
66 back-projection aims at tracking the areas of the source that generate the strongest
67 high frequency radiation, based solely on the phase and the coherency of seismic
68 array signals. This provides robust constraints on the spatio-temporal evolution of the
69 earthquake rupture, without relying on assumed Green's functions nor on restrictive
70 parameterizations of the rupture kinematics. We back-projected P wave seismic
71 waveforms recorded by two large arrays at teleseismic distances, the USArray and the
72 European network, that illuminate the fault from two orthogonal directions (Figure 1).
73 We filtered the waveforms from 0.5 to 1 Hz and applied three different array
74 processing techniques: cubic-root stacking [*Rost and Thomas, 2002*], a classical
75 beamforming technique; Multiple Signal Classification (MUSIC) [*Goldstein and*
76 *Archuleta, 1991; Schmidt, 1986*], a high-resolution technique designed to resolve
77 closely spaced simultaneous sources; and correlation stacking [*Borcea et al., 2005;*
78 *Fletcher et al., 2006*], a technique known to improve robustness in the presence of
79 scattering. The detailed descriptions of the techniques are included in the auxiliary
80 material. Our results based on these three techniques are mutually consistent (Figures
81 1, 2, S1 and S2). Nevertheless, we found that MUSIC consistently yields a sharper
82 image of secondary features of the rupture process. We back-projected the estimated
83 directions of arrival onto the source region at a reference depth of 15 km using
84 differential travel times relative to the hypocentral travel time, based on the IASP91
85 Earth model. The results we obtain with the two arrays are consistent. Remaining
86 differences can be attributed to directivity effects, to interference patterns between

direct and depth phases and to geometrical properties of the isochrones [*Bernard and Madariaga, 1984; Spudich and Frazer, 1984*]. Owing to its larger aperture, the European array provides a sharper image of the rupture process. Our synthetic tests based on empirical Green's functions (**Figures S4-S7**) show that our back-projection imaging can capture the key features of the rupture process of the Tohoku-Oki earthquake highlighted next.

2. High resolution array analysis using USarray and European Network

Figure 1-a shows the location of the regions of strongest HF radiation within 10 seconds long sliding windows. Secondary sources are often visible in our back-projection images, for instance in Figure 3 between 60 and 90 seconds. However, our focus here is on first order features that we can reliably identify by tracking the most coherent phase within each time window. The HF radiation area extends bilaterally over 300 km along strike, roughly one third to the NNW direction and two thirds to the SSE. It bridges over the rupture area of several historical earthquakes off-shore Miyagi and Fukushima that were previously thought to define the segmentation of this subduction interface. The HF rupture is mostly located landwards from the hypocenter, near the down-dip end of the seismogenic zone of the megathrust interface determined from the spatial distribution of megathrust seismicity in the last decades [*Igarashi et al., 2001*]. Figure 1-a also shows the spatial distribution of coseismic slip averaged over a large collection of possible models constrained by geodetic (GPS) and tsunami (DART buoy) data in a Bayesian

framework [Simons *et al.*, 2011]. The locations of HF sources correlate with the down-dip edge of the main slip area. While coseismic slip inversions produced by different teams differ significantly, the spatial complementarity between low and high frequency slip is a common feature well illustrated by this particular slip model. Kinematic source inversions constrained by global teleseismic data, which are dominated by frequencies lower than 0.1 Hz for this earthquake, also place most of the low frequency (LF) slip updip from the hypocenter [Shao *et al.*, 2011]. We found no secondary HF source between the trench and the hypocenter. Moreover, our back-projection analysis at lower frequencies, down to 0.125 Hz (Figure S8), does not show a conclusive trend towards shallower slip. This suggests that slip in the shallower regions of the megathrust interface generated much weaker seismic wave radiation at periods shorter than 10 s, likely related to a longer rise time.

3. The spatio-temporal evolution of the Tohoku earthquake

The spatio-temporal evolution of the strongest HF radiations is indicated in Figure 1-a. Sustained and energetic HF radiation is reliably imaged by our array back-projections during the first 150 seconds of the rupture. The overall HF rupture size during this period indicates a low average rupture speed. However, rupture speed was highly variable, with several stages of slow, fast and extremely fast rupture. A summary plot of rupture time as a function of epicentral distance, shown in Figure 2, provides a more quantitative appreciation of the rupture speed and allows the identification of several distinct stages of the rupture process. Finer details can be observed in the

back-projection imaging snapshots (Figure 3) and movies ([Animation S1 and S2](#)), including simultaneous but weaker HF sources. The HF rupture initially propagates down-dip for about 100 seconds, and then splits up into bilateral rupture along strike. The down-dip propagation stage starts with a slow phase, stalling in the hypocentral region for about 10 seconds (phase 1 indicated in Figure 2), and culminates in a definite change of rupture speed. In the subsequent stage rupture propagates towards the West at usual speeds of order 3 km/s for about 20 seconds (phase 2). The rupture then slows down to less than 1 km/s for about one minute (phase 3). The complex structure of this slow stage is most clearly visualized in the back-projection movies derived from the European array ([Animation S2](#)). The rupture appears as a rich sequence of bursts generated along the rim of a slowly expanding circular front. The slow front is centered significantly down-dip from the hypocenter, which produces episodes of apparent back-propagation. By the end of the slow stage, at about 80 seconds, an extremely fast rupture detaches towards the North, with apparent supershear speed of order 5 km/s (phase 4). Finally a fast rupture front propagates towards the South running at speeds of order 2.5 km/s for more than 100 km (phase 5).

4. Signatures of the rupture process in the strong motion data

We inspected the near-source ground motions recorded by dense strong motion networks in Japan to identify the local signature of the features we observed at teleseismic distances. We analyzed recordings of 64 surface and 42 borehole

accelerometers located along the north-eastern coast of Honshu. We band-passed filtered the traces in various frequency bands, integrated to velocity and computed smoothed S wave energy envelopes (**Figure S9**). Figure 4 shows 5-10 Hz envelopes as a function of station latitude. Amplitudes are normalized to emphasize the arrival time moveout of the main strong motion phases. Three episodes are prominent, two in the North, consistent with sources near the hypocentral latitude, and one far South near the end of the rupture. We trace rays from the HF source locations determined by the back-projection analysis to the strong motion stations, using a 1D velocity model derived from local seismic profiles [Takahashi *et al.*, 2004]. The three prominent bursts are thus associated to HF phases observed at teleseismic distances. The colored vertical short bars in Figure 4 indicate the S-wave arrival times from locations that ruptured 33, 85 and 140 seconds after the mainshock origin time. These correspond, respectively, to the end of the first fast rupture stage, the beginning of the extremely fast northwards rupture and the approach to the southern end of the rupture. The strong motions are intermittent in Miyagi and more sustained along Fukushima, reflecting the contrasted character of these two portions of the rupture.

5. Discussion

Our results highlight the spatial complementarity between low and high frequency source properties of the Tohoku earthquake, as also discussed elsewhere [Simons *et al.*, 2011]. This phenomenon has been reported for several other earthquakes, although not systematically [Nakahara, 2008]. Possible explanations include the presence of

frictional heterogeneities in the brittle-ductile transitional regions at the base of the seismogenic zone, stopping phases radiated from abrupt rupture arrest, strong phases radiated when the rupture front encounters residual stress concentrations left by previous earthquakes [*Madariaga, 1983*] and dynamic triggering of crustal faults above the mega-thrust. A natural generalization of this HF/LF complementarity to intermediate frequencies poses a cautionary note for source inversion studies that combine geodetic and seismological data, which are sensitive to different frequencies. The relation between HF and LF source radiation also provides an observational constraint on kinematic source models for broadband ground motion prediction and urges for the integration of physics-based rupture models into those methodologies [*Pulido and Dalguer, 2009*].

Our analysis reveals the seismic signature of a slow initiation of the Tohoku-Oki earthquake rupture. Back-projection of the initial portions of the waveforms was done with shorter (5 s long) sliding windows to unambiguously resolve the existence of this (roughly 10 s long) slow initiation phase. A progressive transition to dynamic rupture has been observed in laboratory experiments [*Nielsen et al., 2010; Ohnaka and Kuwahara, 1990; Okubo and Dieterich, 1984*] and predicted by theoretical models [*Ampuero and Rubin, 2008; Dieterich, 1992; Lapusta and Rice, 2003*], but has eluded unambiguous seismological observations at natural scales. Whether this initiation stage is subtended by an aseismic nucleation process or results from a cascade of triggering between seismic subevents [*Ellsworth and Beroza, 1995*], cannot be

resolved by our analysis. The duration of the observed slow initiation stage (order 10 s) is consistent with the empirical scaling relation between nucleation phase duration and seismic moment proposed by [Ellsworth and Beroza, 1995], although somewhat shorter suggesting a break in scaling at very large magnitudes possibly due to saturation of the seismogenic depth. Further studies of the nucleation of the Tohoku earthquake are warranted, including imaging of its early stages based on empirical Green's functions [Shibazaki *et al.*, 2002; Uchide and Ide, 2007] and analysis of its foreshock sequence [Bouchon *et al.*, 2011].

During the second slow rupture stage of the Tohoku earthquake (phase 3 in Figure 2), the macroscopic rupture front almost comes to a halt and then restarts. This stage provides another potential window into the factors controlling earthquake nucleation and arrest, especially under transient stressing conditions. A similar slow rupture stage with apparent speed of order 1 km/s was inferred between two main asperities during the 2007 Pisco earthquake, off-shore Peru [Perfettini *et al.*, 2010]. However, the scarcity of data recorded for that event did not allow to resolve whether the long delay between the two main subevents was due to a slow rupture or to a delayed triggering process. For the Tohoku earthquake the migration pattern of the HF radiation during the slow stage is consistent with triggering along the rim of a slow rupture front. This slow stage could be related to propagation over a transition region between brittle and ductile fault behavior that separates the hypocentral region from the slip regions of the 1978 and 2005 Miyagi-Oki earthquakes. We picture this as a rheologically

heterogeneous region made of a ductile fault matrix interspersed by compact brittle asperities capable of generating HF radiation. This patchy view of the brittle-ductile transition zone is consistent with the observation of clusters of repeating earthquake in Tohoku [Igarashi *et al.*, 2001], and is analogous to a current interpretation of the environment where coupled slow slip and tremor processes occur [Ito *et al.*, 2007]. In an alternative interpretation the rupture slowed down as it propagated over regions of low stress within the slip area of the 1978 and 2005 Miyagi earthquakes, but radiated HF as it hit the stress concentrations left at the edges of those same events. Similarly, the final rupture stage towards the South delineates the bottom edge of historical earthquakes off-Fukushima. Yet another possibility is that these HF bursts originated from coseismically triggered shallow crustal faults. A finer resolution study of the depth and focal mechanism of the HF sources, aftershocks and repeating earthquakes might help discriminating these interpretations.

The stage of extremely fast rupture towards the North is most clearly visible by the European array, which has better resolution in the along-strike direction. This stage could correspond to a supershear rupture front. Its speed is comparable to $\sqrt{2}$ times the S wave speed, a stable speed in dynamic models of supershear rupture [Rosakis, 2002]. A subshear front hitting obliquely into a barrier is an alternative interpretation, but that would generate an apparent speed in the observed range only under very restrictive conditions. Alternatively, dynamic triggering would create an apparent supershear phenomena, since the back-projection tends to image apparent secondary

sources with small power connecting true sources ([Figure S7](#)). This artifact is unlikely for the Tohoku-Oki earthquake, since the power is almost uniform during the supershear stage. However, the very fast front propagates mainly along strike and existing theoretical models do not allow supershear ruptures in mode III. Along-strike supershear rupture in subduction earthquakes requires a significant along-strike slip component or yet unexplored mode coupling processes that efficiently break the mode III symmetries. While the second strong phase observed in the strong motion data can be associated to the HF radiation found in dynamic rupture models during the transition to supershear speeds, this is not a unique interpretation. Further signatures of supershear propagation might be found in the local strong motion data if there is significant Mach cone radiation towards the land. Ocean bottom pressure gauges that recorded HF acoustic signals, especially stations TM1 and TM2, could also provide precious insight into this question.

Our observations provide an overview of the complicated rupture process of the Tohoku-Oki earthquake and virtually constitute, in a single event, a catalog of the broad spectra of earthquake phenomenology. We highlighted here key features of relevance for earthquake dynamics. These are potential targets for further efforts to assimilate the wealth of data related to this mega-earthquake, with the ultimate goal of understanding the relations between earthquake complexity and the heterogeneous and multi-scale structure of active fault zones.

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Figure captions

Figure 1. Tohoku-Oki earthquake imaged by the USarray and European network. (a) location of the strongest high frequency radiators of the Tohoku-Oki earthquake, seen by the USarray (squares) and by the European network (circles). The color denotes the timing with respect to the origin time. The size of the symbols denote the relative amplitude of the radiators. The black contours map the average slip distribution constrained by geodetic and tsunami data

[Simons *et al.*, 2011]. The green ellipses represent the approximate rupture zone of the historical earthquakes. The pink line near the coast indicates the down-dip limit of the megathrust seismicity [Igarashi *et al.*, 2001]. The inset map shows the location of the two arrays with respect to Japan. **(b)** location of the 291 USarray and 181 European stations selected for our back-projection analysis.

Figure 2. Rupture time versus epicentral distance. The timing of the high frequency radiators seen by both arrays are plotted against their epicentral distance. The color denotes their azimuth with respect to the epicenter and the size of the circles denotes their relative amplitude normalized by the maximum amplitude during the event. The numbers in circles mark the five phases with distinct rupture behavior discussed in section 3. The left panel shows the temporal evolution of normalized amplitudes estimated at the USarray (blue) and at the European network (red).

Figure 3. Back projection images every 20 seconds. Colors show the amplitude of the MUSIC pseudo-spectrum. The warmer colors indicate the location of the dominant high frequency radiation sources. The additional snapshot at 90 seconds contains a supershear front to the north. The red star denotes the mainshock epicenter and small white dots the epicenters of aftershocks with magnitude larger than 6 within the first two days. The thick white line represents the trench.

Figure 4. Signatures of the rupture process in the near-source strong motion recordings.

374 Smoothed high-frequency (5-10 Hz) horizontal energy envelopes of strong motion data
375 recorded along the north-eastern coast of Honshu. The selected stations are shown by
376 triangles in the inset map. Traces are scaled by their maximal amplitude. Red, yellow and
377 green vertical bars along the time series indicate the S-wave travel times from high-frequency
378 sources inferred by the back-projection analysis. These ruptured 33s, 85s and 140s after the
379 mainshock origin time, respectively. Their locations are indicated by squares of the respective
380 color in the inset map. The stars denotes the mainshock epicenter.

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